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# Single-frequency, TEM<sub>00</sub>-mode Nd:YLF laser with image - rotation resonator

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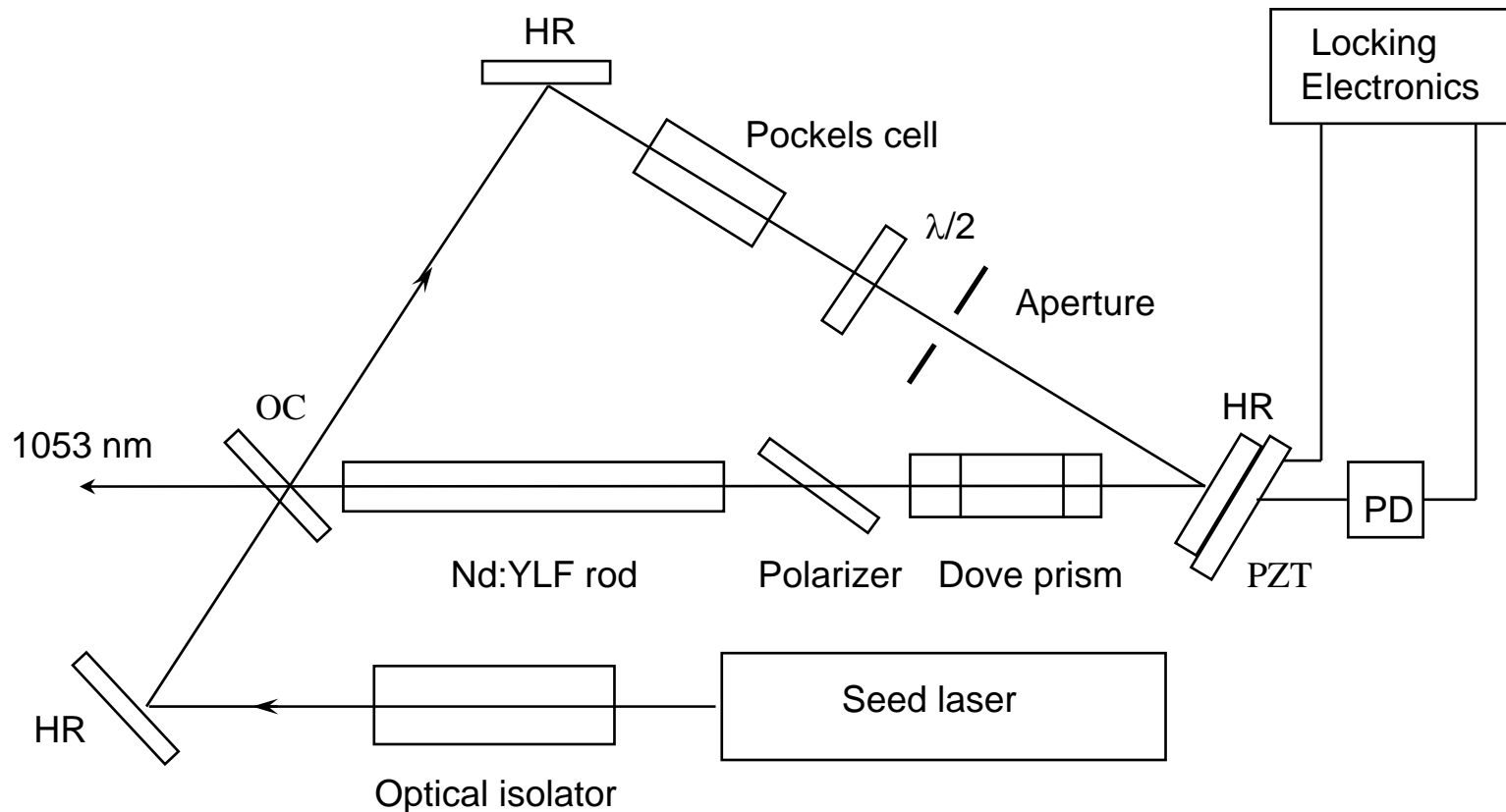


# Outline

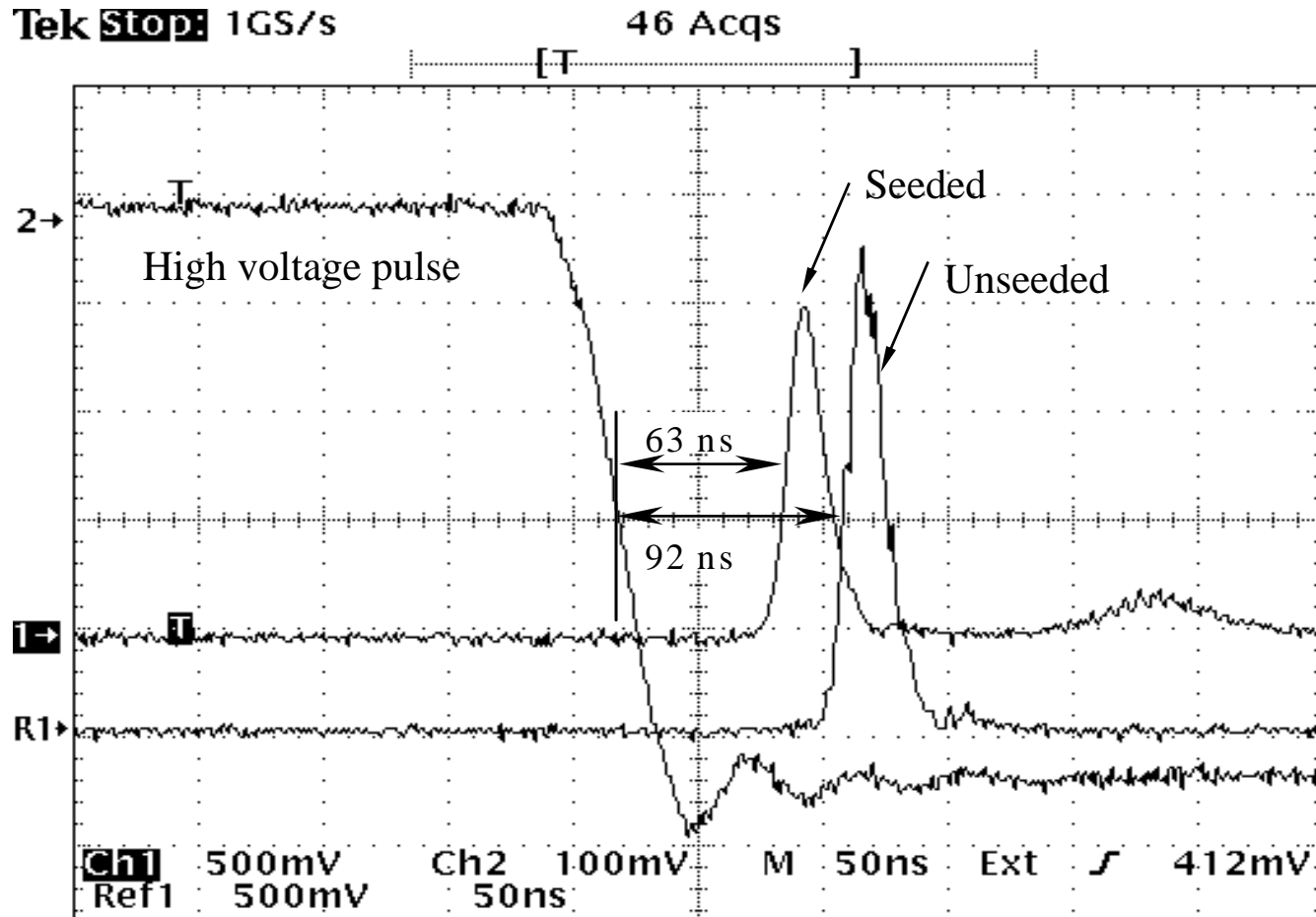
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- Image-Rotation (IR) resonator setup
- Injection-locking technique based on a pulse buildup time control
- Alignment sensitivity of IR resonators
- Polarization losses of IR resonators
- Transverse mode selection in IR resonators
- $90^\circ$  -IR,  $N=3$  Laser performance
- Summary

# Q-switched Nd:YLF ring laser with image rotation and injection locking



# Oscilloscope traces of the HV- and laser pulses



# Image Inversion and Rotation in Ring Resonators

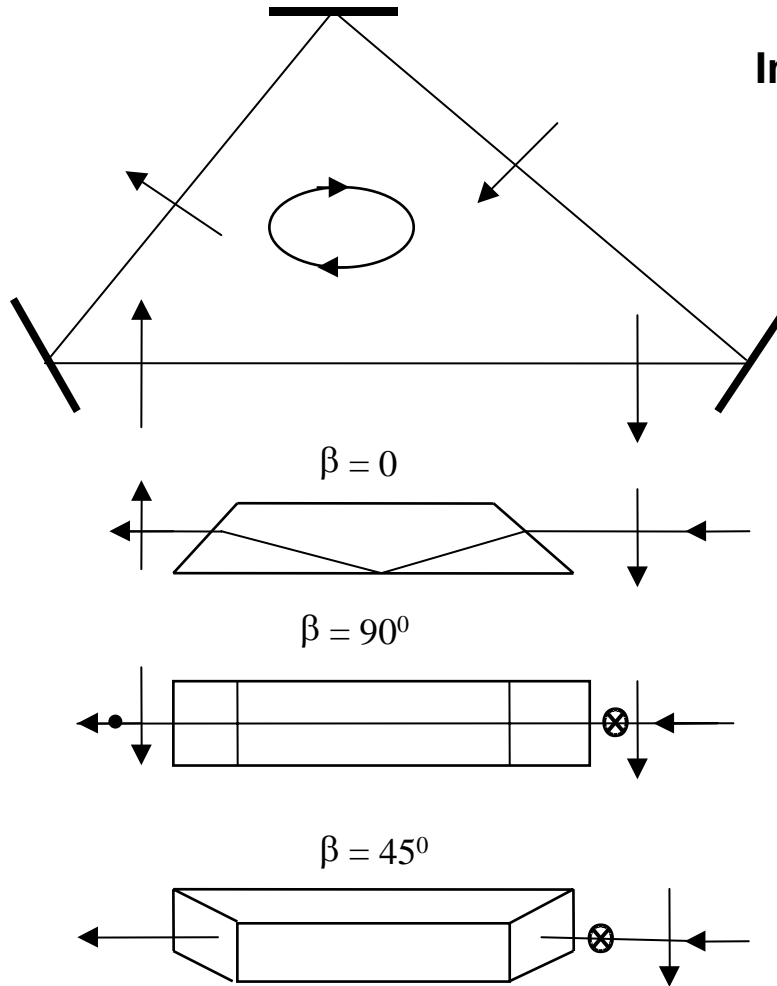
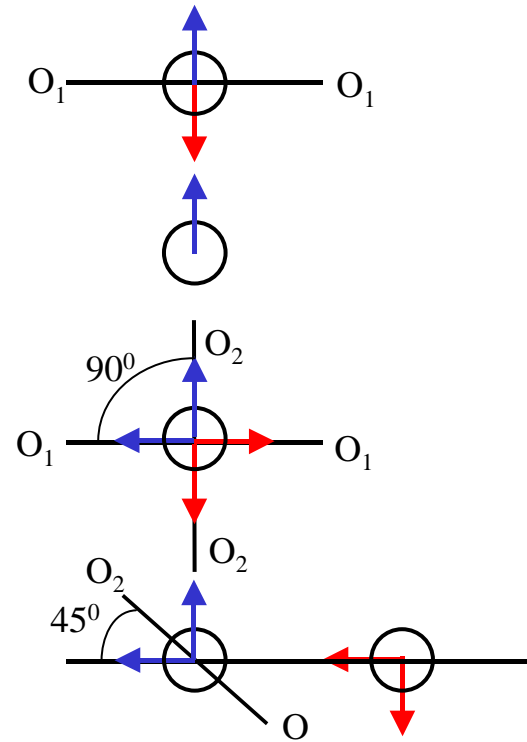


Image rotation angle,  $\Omega$ , is twice the angle between inversion axes, i. e.

$$\Omega = 2\beta$$



# Alignment Sensitivity of the Image Rotation Resonators

$$x_0 = -L \varphi_x / (1 - \cos \Omega)$$

$$\alpha_{x0} = -\varphi_x - \varphi_y \sin \Omega / 2 (1 - \cos \Omega)$$

$$y_0 = -L \varphi_y / 2 (1 - \cos \Omega)$$

$$\alpha_{y0} = \varphi_x \sin \Omega / (1 - \cos \Omega) - \varphi_y / 2$$

$x_0, y_0, \alpha_{x0}, \alpha_{y0}$  - coordinates of the axis of the misaligned resonator

$$\Omega = 180^\circ$$

$$x_0 = -L \varphi_x / 2$$

$$\alpha_{x0} = -\varphi_x$$

$$\Omega = 90^\circ$$

$$x_0 = -L \varphi_x$$

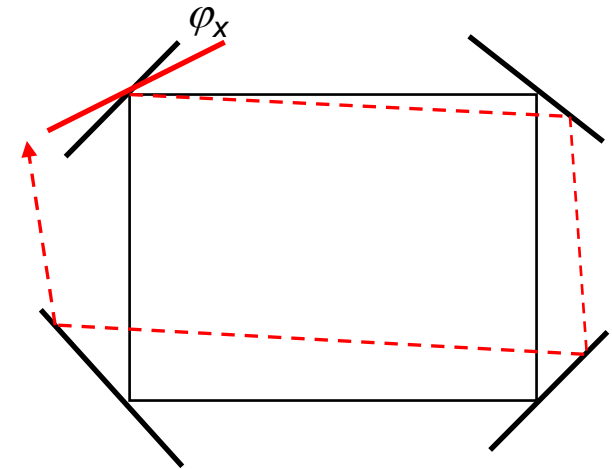
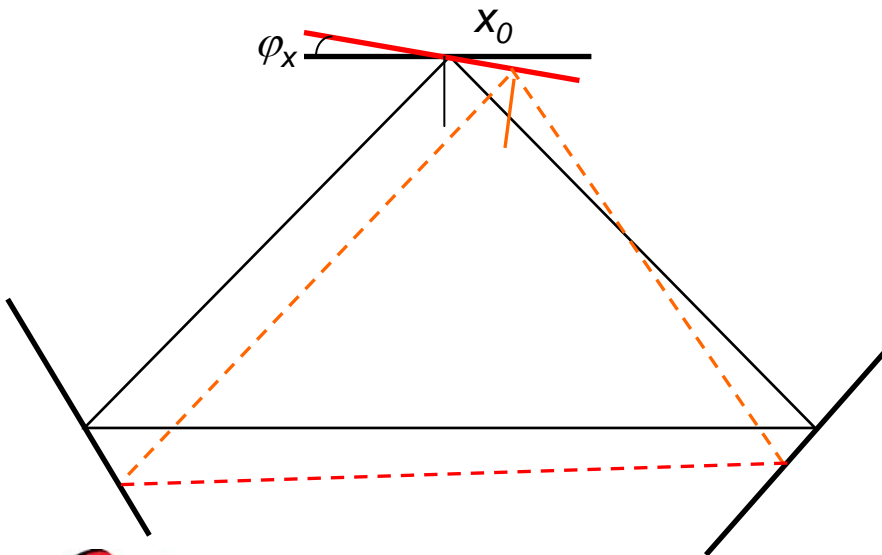
$$\alpha_{x0} = -\varphi_x$$

$$\alpha_{y0} = \varphi_x$$

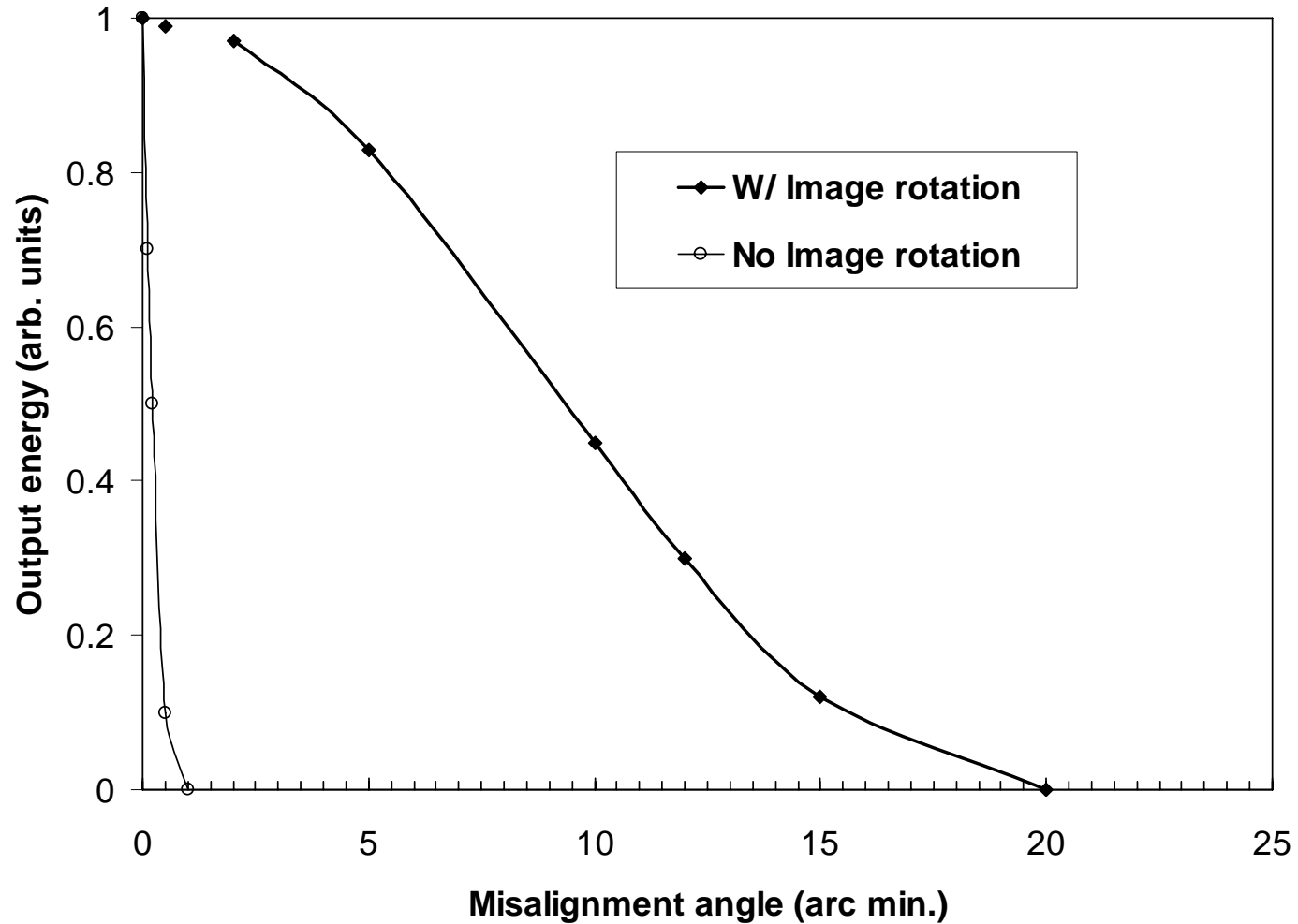
$$\Omega = 0$$

$$x_0 = \infty$$

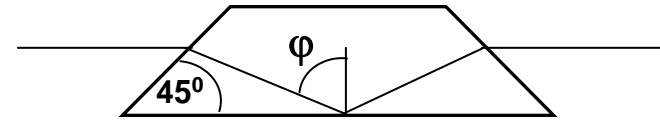
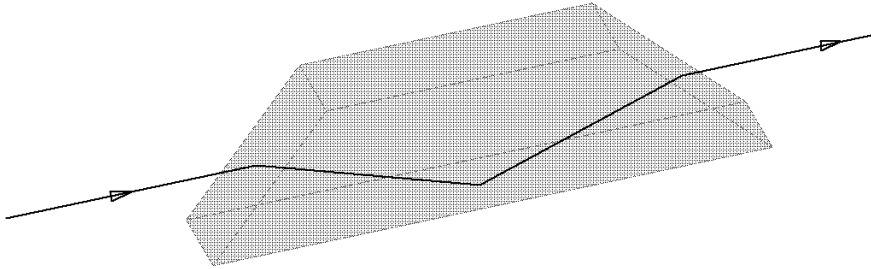
$$\alpha_{x0} = -\varphi_x$$



# Misalignment Tolerance of Different Resonators



# Polarization Properties of IR-Resonators



*Transformation of polarization caused by a Dove prism :*

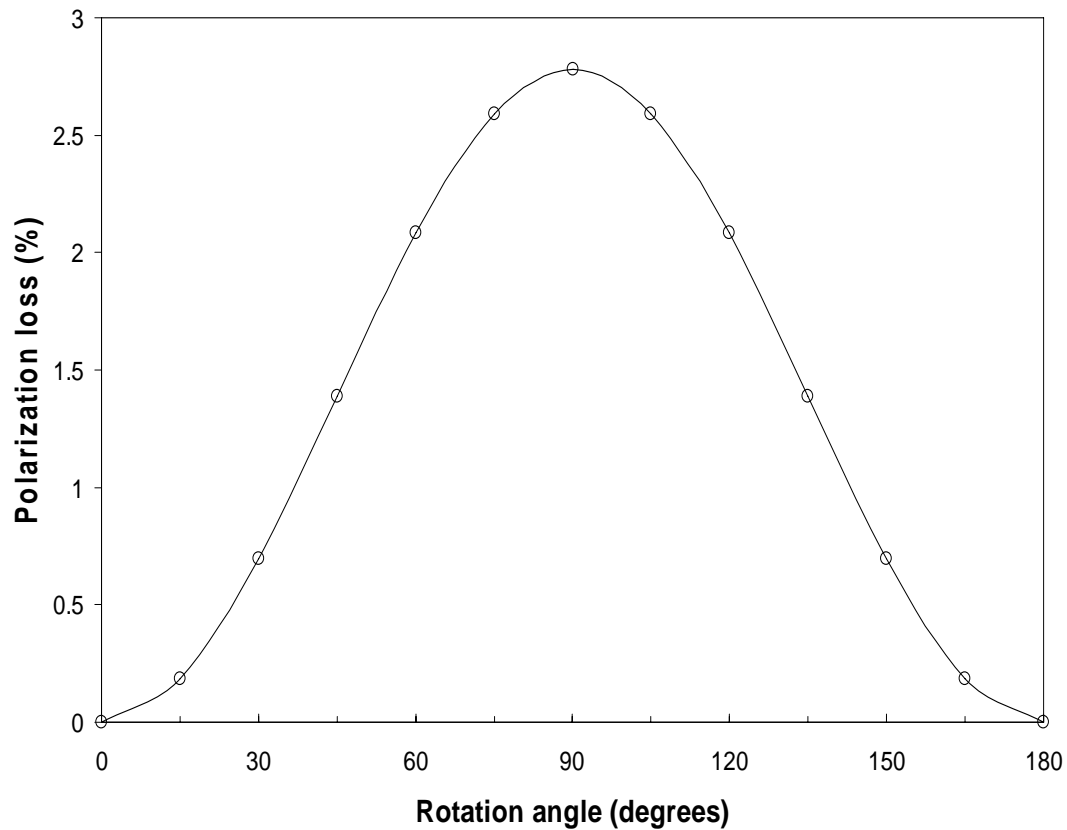
$M(-\beta) M(\delta) M(+\beta)$ , where

$$\tan (\delta / 2) = \sqrt{\sin ^2 \varphi - n^{-2}} / \sin ^2 \varphi$$

$$M(\beta) = \begin{bmatrix} \cos \beta & \pm \sin \beta \\ \mp \sin \beta & \cos \beta \end{bmatrix}, \quad M(\delta) = \begin{bmatrix} e^{(i\delta/2)} & 0 \\ 0 & e^{(-i\delta/2)} \end{bmatrix} \quad J_D = \begin{bmatrix} (1 - e^{-i\delta}) \cos \beta \sin \beta \\ \sin^2 \beta + e^{-i\delta} \cos^2 \beta \end{bmatrix}$$

# Polarization Losses of the IR Resonators

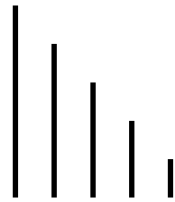
$$\gamma = \cos^2(\delta/2) - \sin^2(\delta/2) \cos^2(2\beta)$$



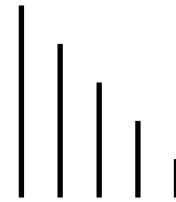
# Transverse mode frequencies in ring stable gaussian resonators

$$\Delta\nu = \left(\frac{c}{L}\right) \left[ \Delta q + \Delta(2p+l) \arccos\left(1 - \frac{L}{R}\right) \right]$$

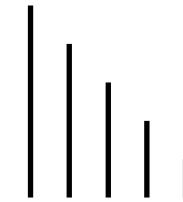
$$\left\langle \Delta\nu = c/L \right\rangle$$



TEM<sub>plq</sub>



TEM<sub>pl(q+1)</sub>

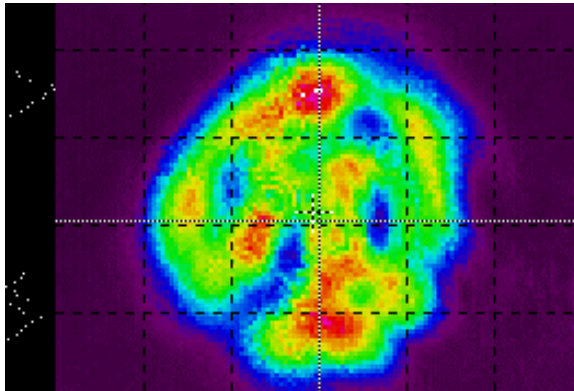


TEM<sub>pl(q+2)</sub>

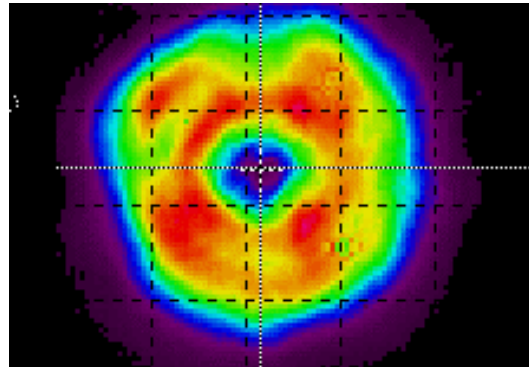
Transverse modes with odd function distribution undergo additional  $\pi$  or  $c/2L$  frequency shift in odd-number-mirror resonators

# Near-Field Beam Profiles of the Ring Resonators (1)

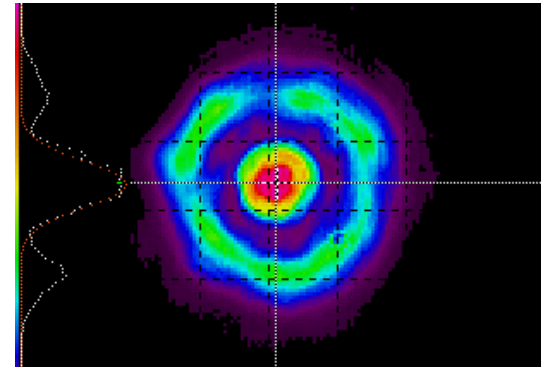
no IR  
N=7



90°- IR  
N=7  
w/seeding

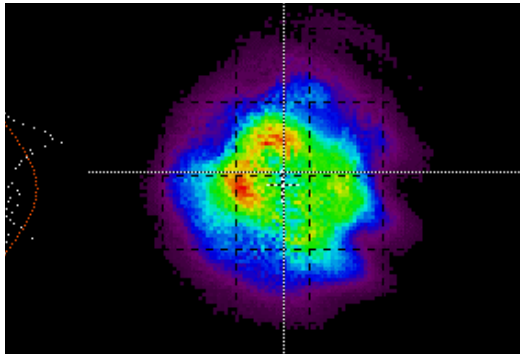


90°- IR  
N=7  
w/seeding

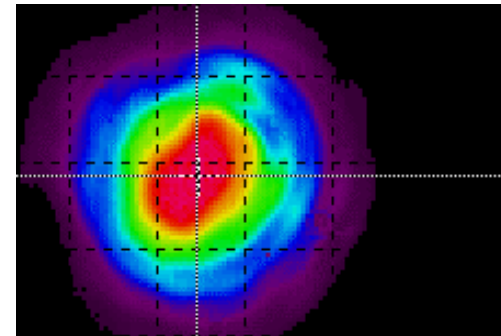


# Near-Field Beam Profiles of the Ring Resonators (2)

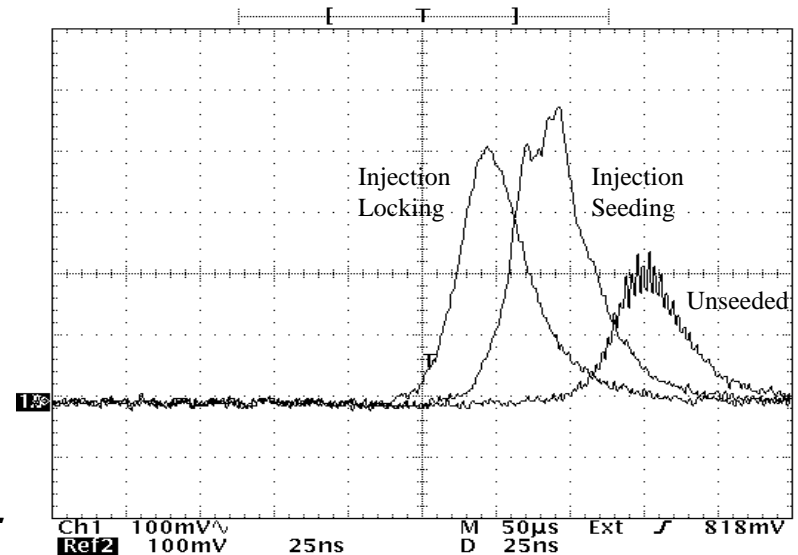
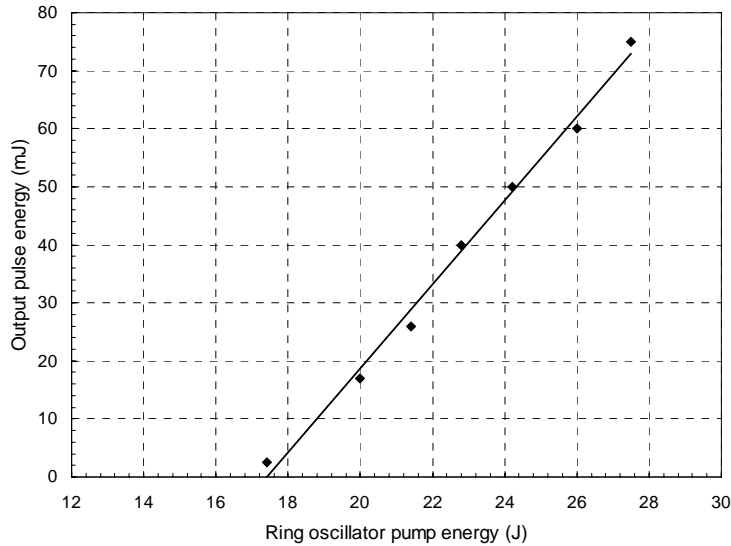
no IR  
N=3



90°- IR  
N=3  
w/seeding



# 90° -IR, N=3 Ring Laser Performance



- Up To 75 mJ output pulse energy
- Single-frequency, near diffraction-limited beam
- $M^2 = 1.33, 1.24$
- 10-30 Hz Repetition Rate

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